

Planning and Control of UGVs in a Dynamic Environment: A Practical Framework with Experiments

Sunil K. Agrawal, Ph.D.

Professor

Department of Mechanical Engineering

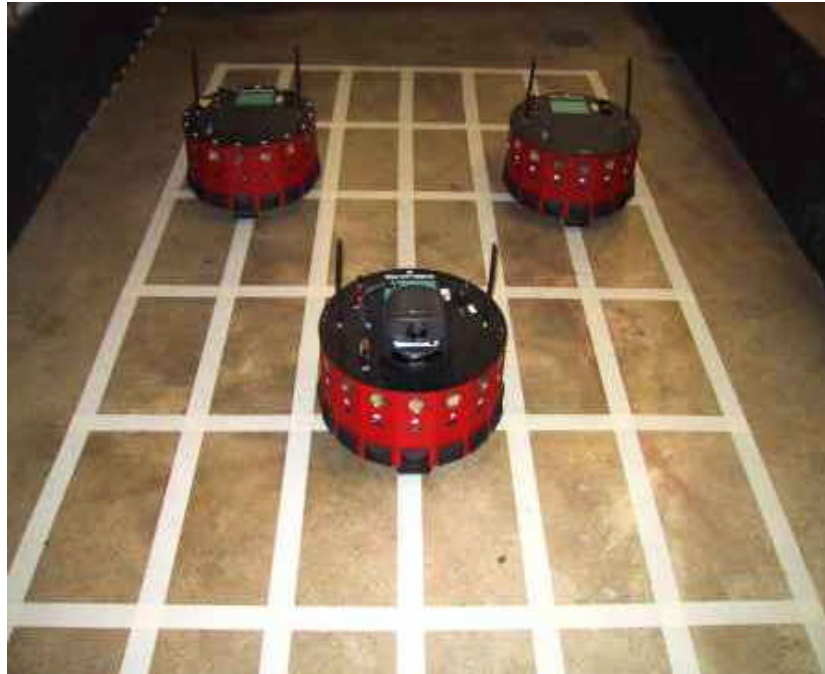
University of Delaware, Newark, DE 19716

Presented by

Stephen Balakirsky, Ph.D.

NIST Intelligent Systems Division

INTRODUCTION



Goal:

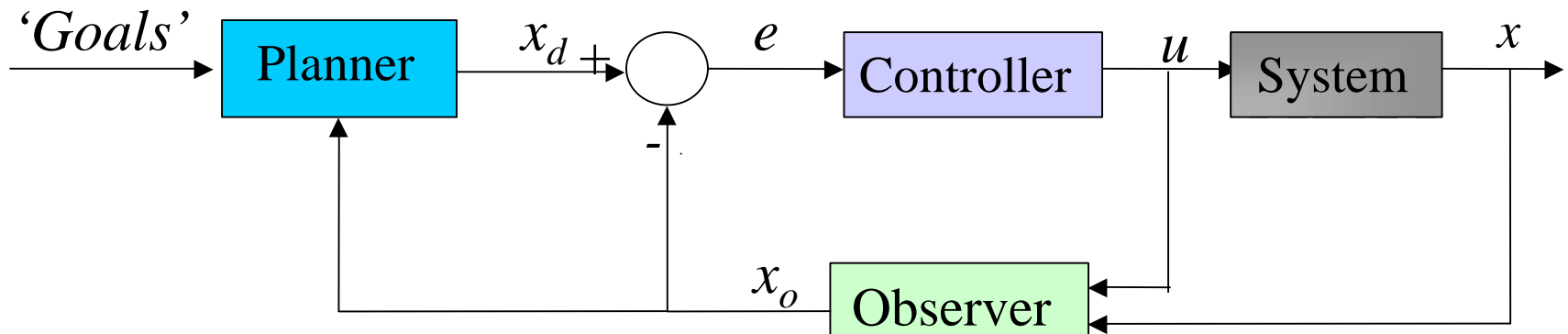
Planning and control of formations of multiple unmanned ground vehicles to traverse between goal points in a dynamic environment

INTRODUCTION



$$\dot{x} = F(x, u)$$

$$x \in \mathbb{R}^n, u \in \mathbb{R}^m$$



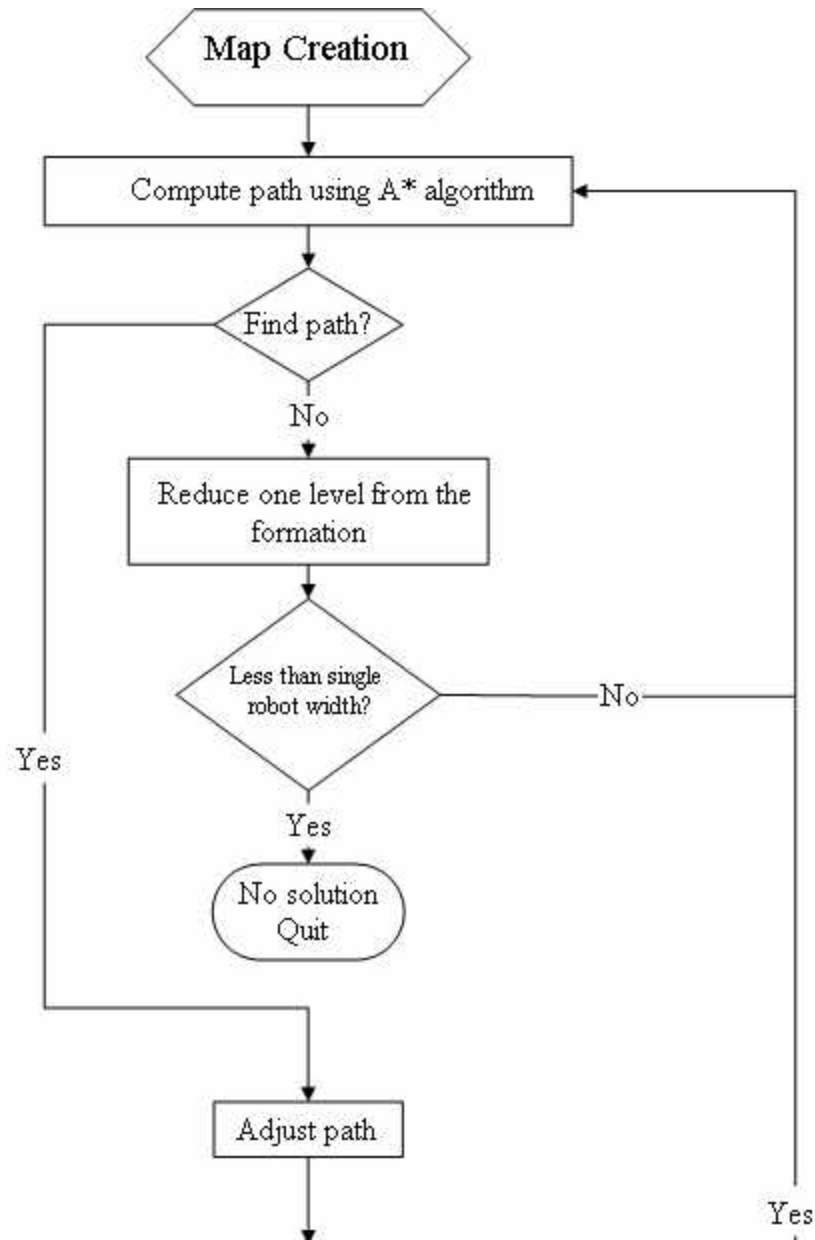
OUTLINE

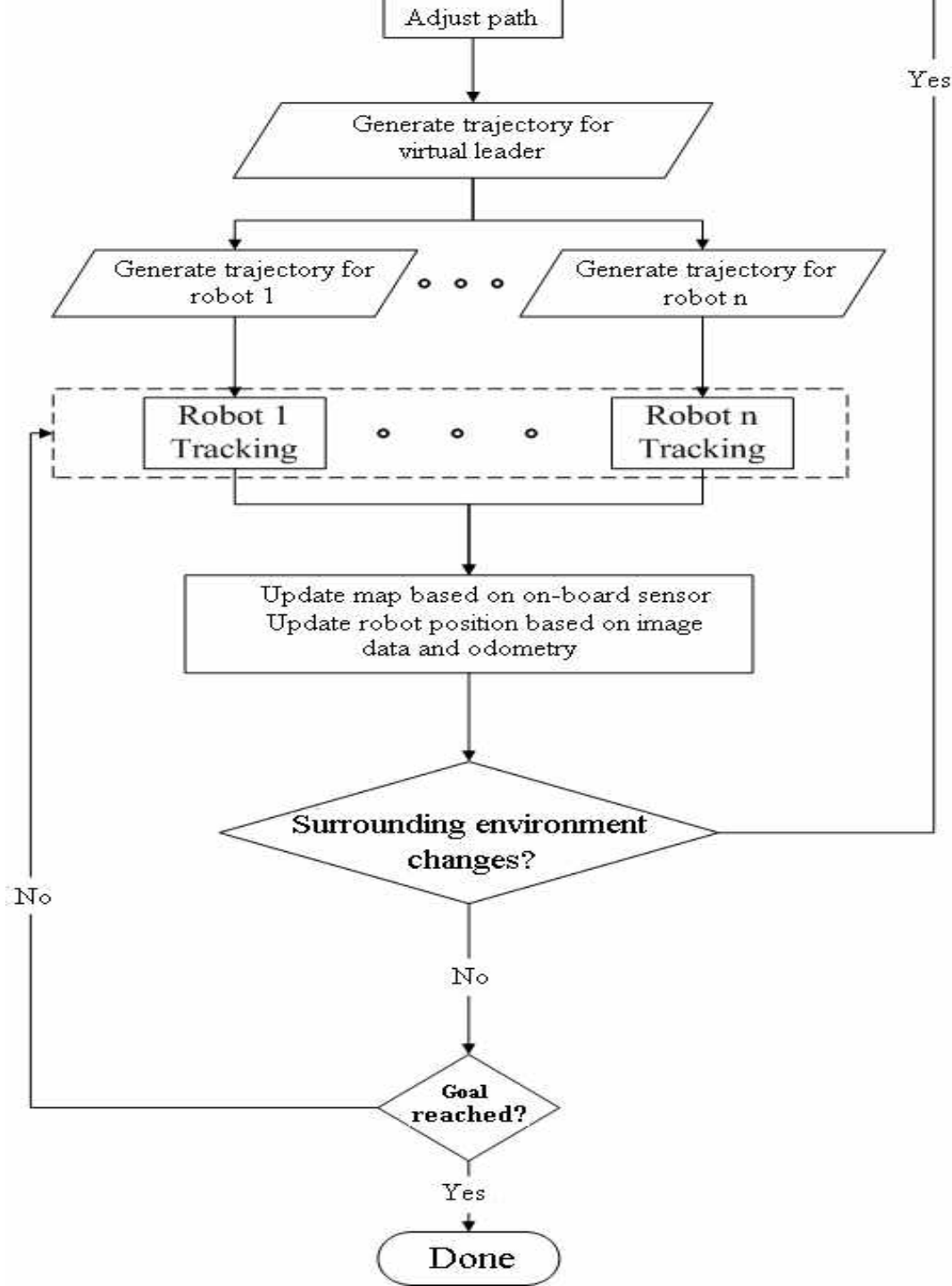
- I. Flowchart
- II. Dijkstra Search – Finding via points
- III. Trajectory Generation and Tracking Controller
- IV. Laboratory Experiments
- V. Formations of UGVs with Trailer
- VI. Conclusions

Assumptions

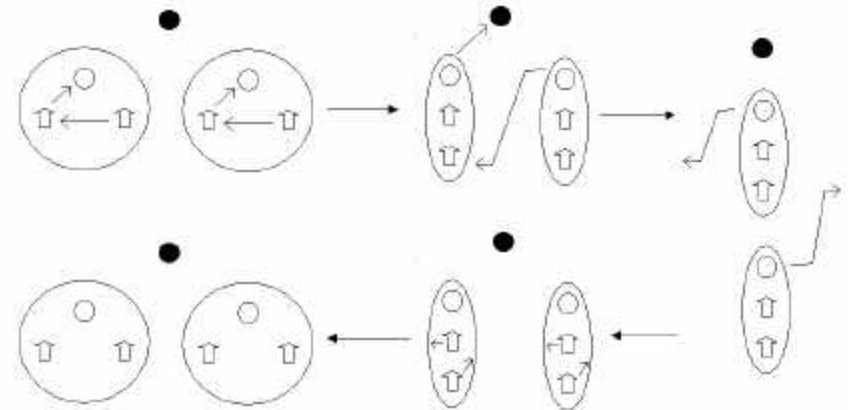
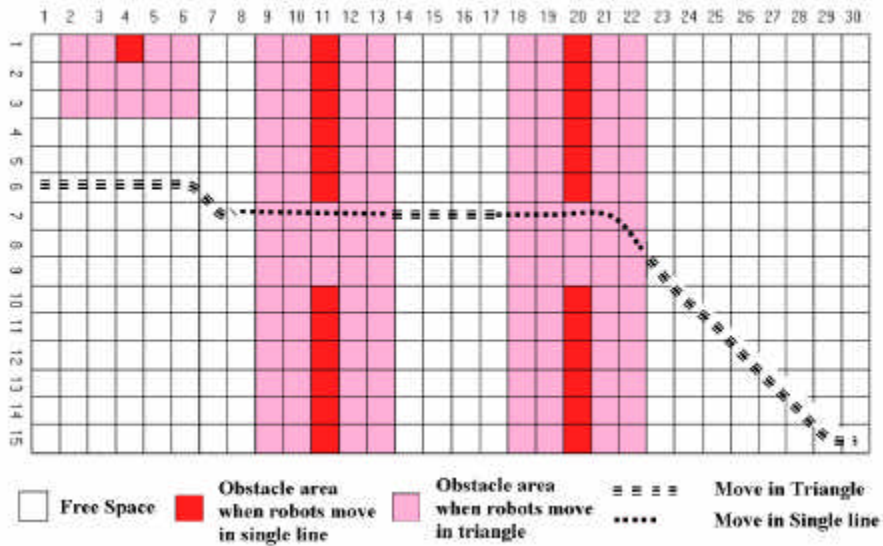
- Robots have on-board sensors, computing, and communication
- Robots change formations recursively to avoid obstacles
- Robot dynamics are accounted during trajectory planning
- Tracking controllers keep the error bounded
- Environment is slowly varying
- UGV's are differentially driven robots with speed commands

Framework



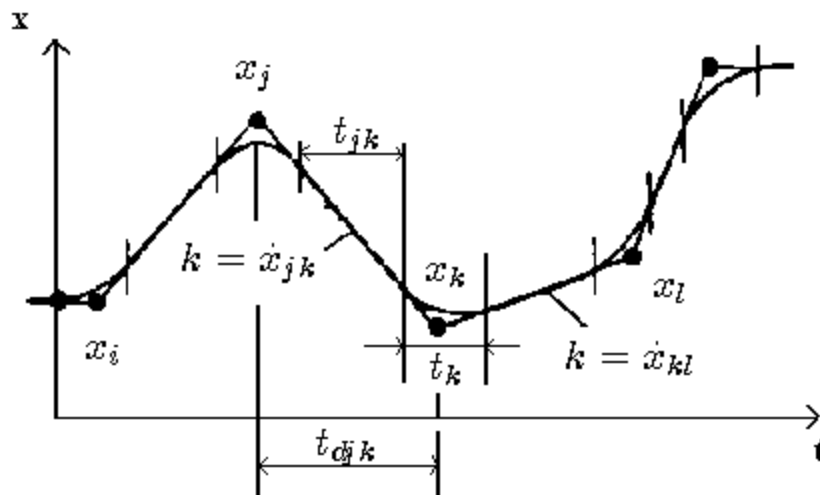


Framework

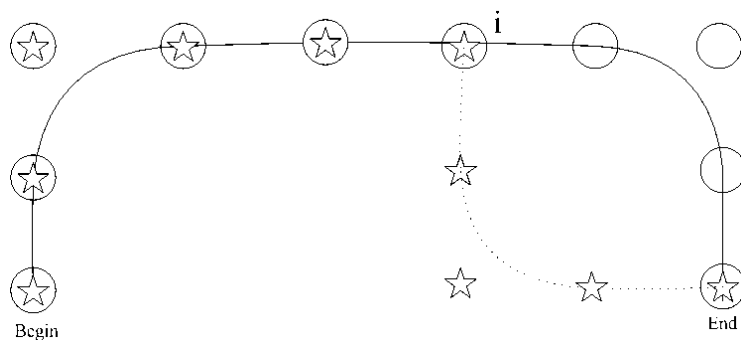


An illustration of a formation change from a tree to a line to a tree.

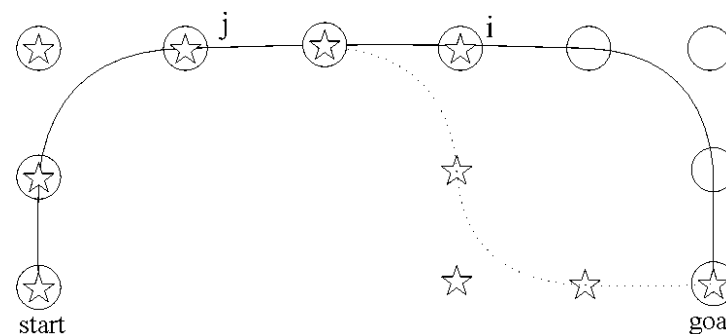
Smooth Trajectory from Via Points



- Interpolating functions
- Use of cubic Splines



Sharp Turning



Smooth Turning

Tracking Controller: Use of Lyapunov functions

Vehicle Model:

$$\dot{x}_i = u_{1i} \cos \theta_i$$

$$\dot{y}_i = u_{1i} \sin \theta_i$$

$$\dot{\theta}_i = u_{2i}$$

Error Model:

$$x_{ei}(t) = x_{ri}(t) - x_i(t)$$

$$y_{ei}(t) = y_{ri}(t) - y_i(t)$$

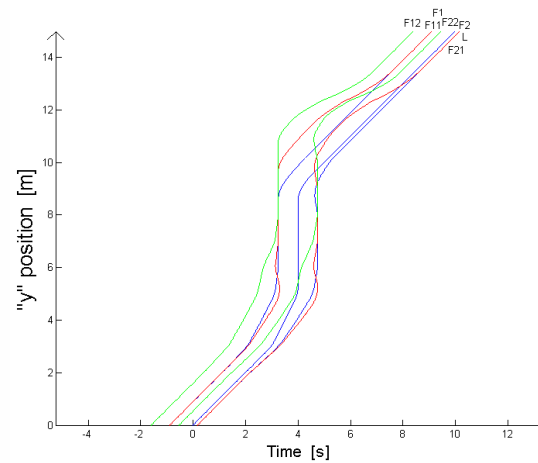
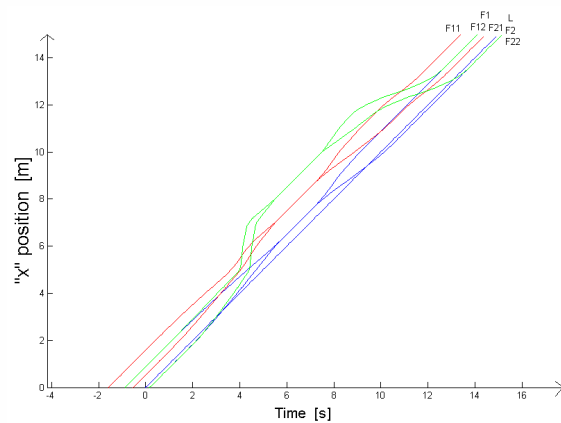
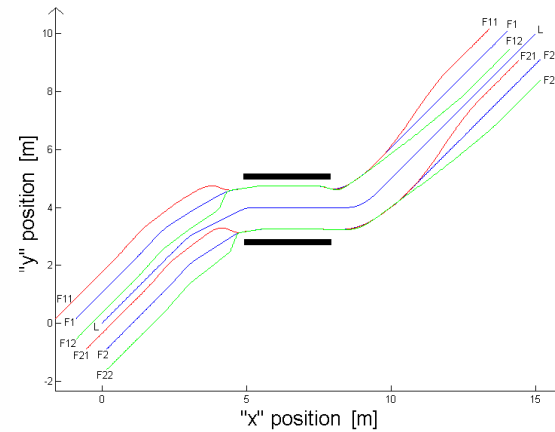
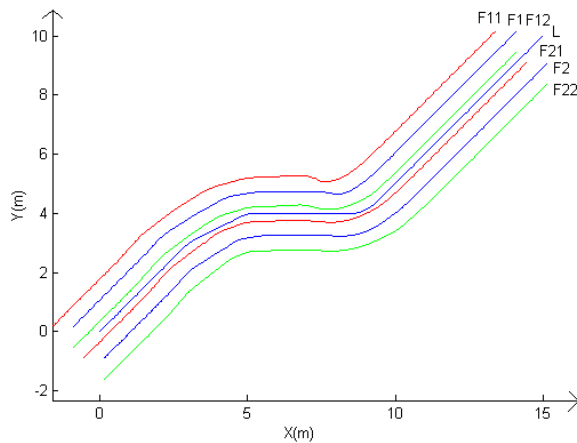
$$\theta_{ei}(t) = \theta_{di}(t) - \theta_i(t)$$

Asymptotically Stable Control Law:

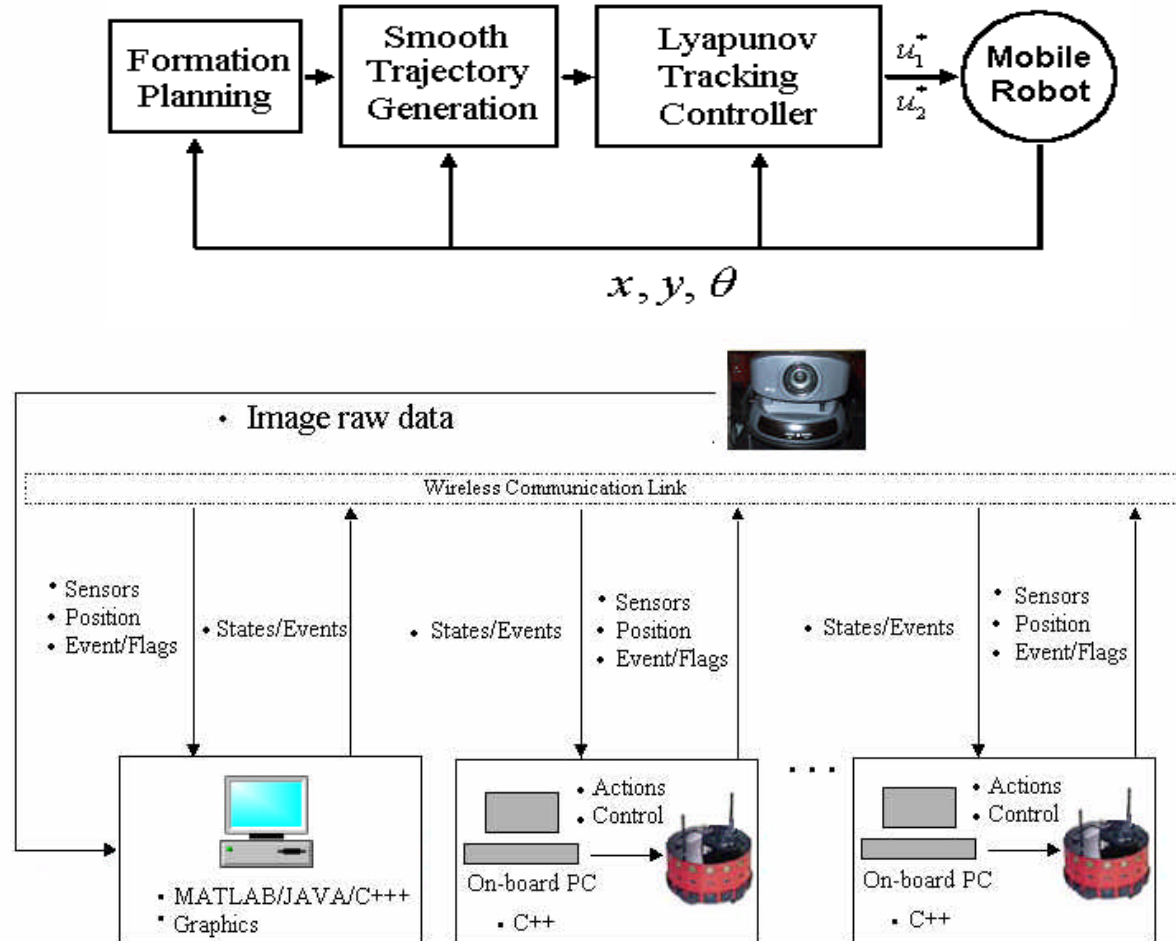
$$u_{1i} = \frac{x_{ei}\dot{x}_{ri} + y_{ei}\dot{y}_{ri}}{x_{ei}\cos\theta_i + y_{ei}\sin\theta_i} + k_{1i}(x_{ei}\cos\theta_i + y_{ei}\sin\theta_i)$$

$$u_{2i} = \frac{x_{ei}(\dot{y}_{ri} - u_{1i}\sin\theta_i) - y_{ei}(\dot{x}_{ri} - u_{1i}\cos\theta_i)}{x_{ei}^2 + y_{ei}^2}$$

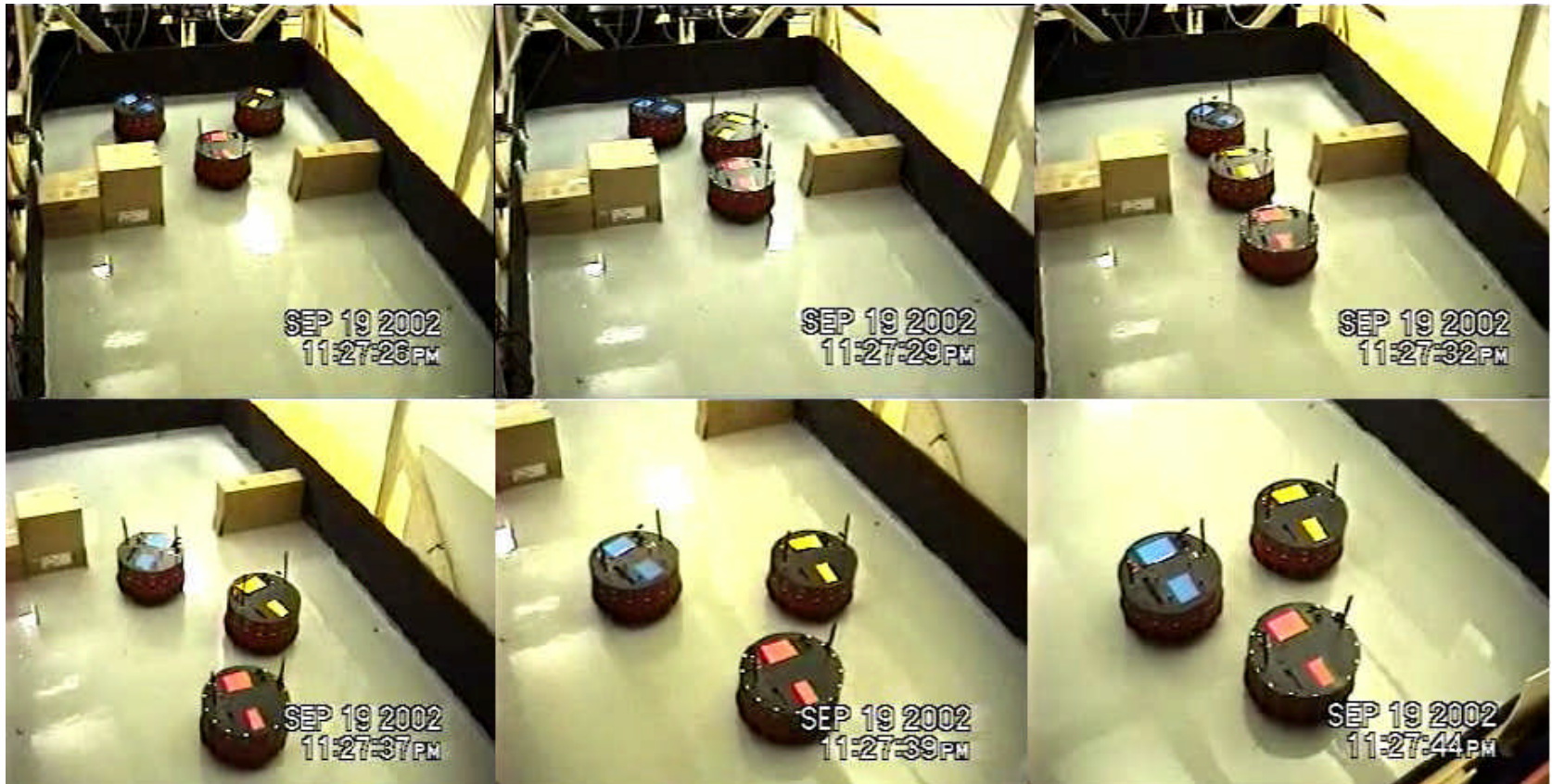
Simulation: Trajectory Generation / Tracking



Laboratory Experiments



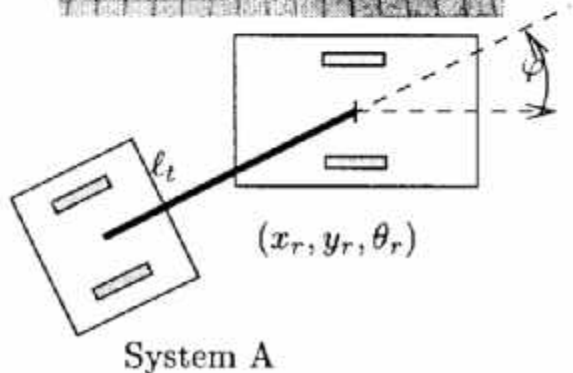
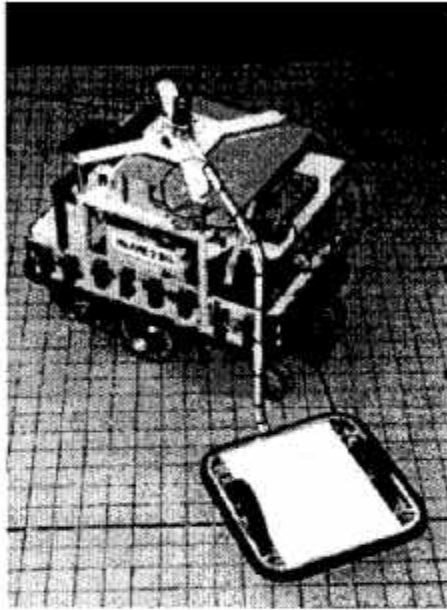
Laboratory Experiments: Snapshots (Movie Follows)



Laboratory Experiments



Control of UGVs with Trailers



- Vehicle Models

$$\dot{x}_r = v_r \cos \theta_r$$

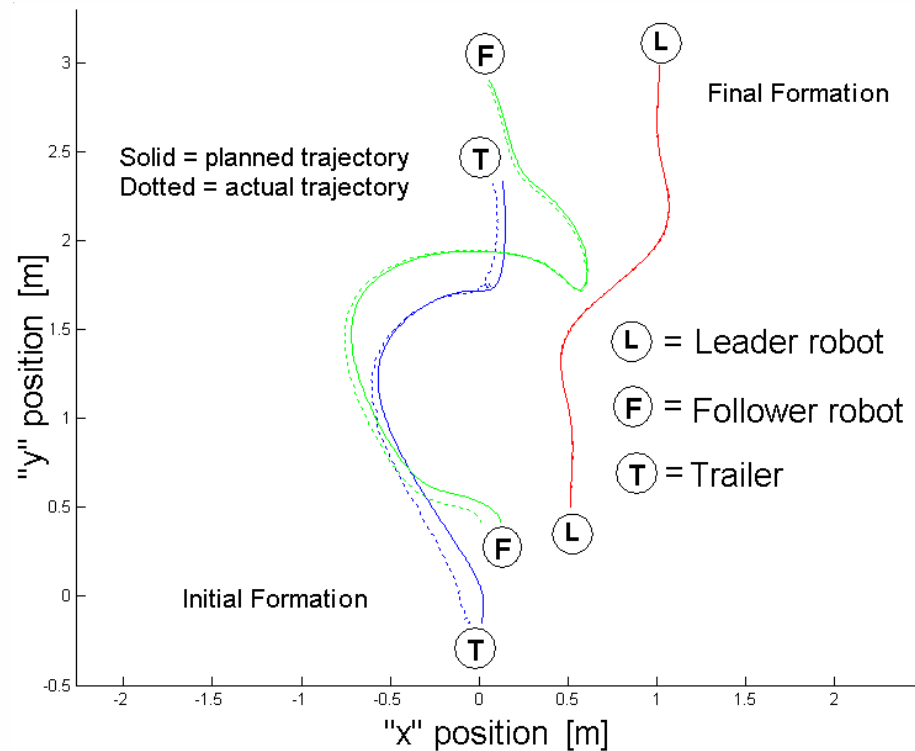
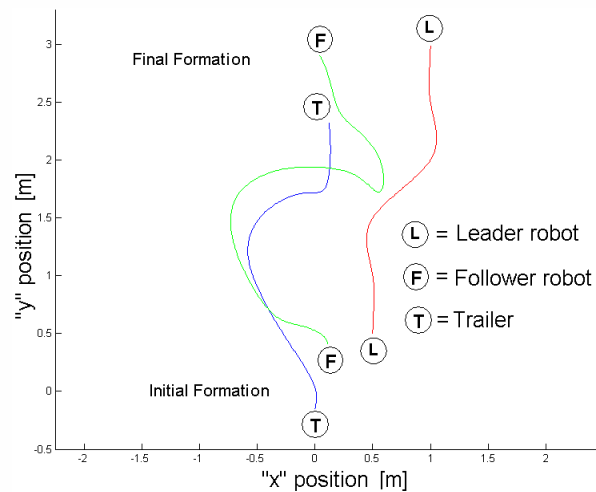
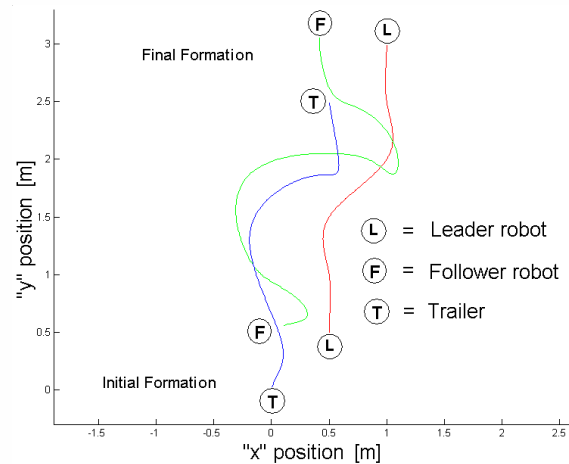
$$\dot{y}_r = v_r \sin \theta_r$$

$$\dot{\theta}_r = \omega_r$$

$$\dot{\varphi} = -\frac{v_r}{l_t} \sin(\varphi) - \frac{l_r \omega_r}{l_t} \cos(\varphi) - \omega_r$$

- Planning and control methods can be simply extended

Simulation of Formations of UGVs with Trailer



Experiment with a UGV/Trailer: (Motivation from crop harvesting)



Conclusions and Planned Work

- A Practical framework is in place for trajectory planning and control of single and groups of vehicles in static and dynamic environments.
- This framework has been tested in laboratory test environment.
- Current plan is to implement this methodology on NIST mobile vehicle platforms and study issues of transfer of this technology for use in industrial environment.